

# REPORT DOCUMENTATION PAGE

AFRL-SR-AR-TR-02-

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering the required information, reviewing and collecting the information, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing the burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paper Project Collection (0141-0297), Washington, DC 20503.

viewing  
information

1. AGENCY USE ONLY (Leave blank)		2. REPORT DATE	3. REPORT TYPE AND DATES COVERED 01 APR 99 -30 NOV 01
4. TITLE AND SUBTITLE Turnable Photonic Crystals			5. FUNDING NUMBERS F49620-99-1-0203
6. AUTHOR(S) Dr. Alex Figotin			
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) University of California, Irvine Department of Mathematics 420 rowland Hall Irvine, CA 92697-3875			8. PERFORMING ORGANIZATION REPORT NUMBER
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES) AFOSR/NM 801 N. Randolph Street Room 732 Arlington, VA 22203-1977			10. SPONSORING/MONITORING AGENCY REPORT NUMBER  F49620-99-1-0203
11. SUPPLEMENTARY NOTES			
12a. DISTRIBUTION AVAILABILITY STATEMENT APPROVED FOR PUBLIC RELEASE, DISTRIBUTION UNLIMITED			
13. ABSTRACT (Maximum 200 words) Our initial theoretical work with Dr. Yu. Godin on asymptotic models for 3D thin-film photonic crystals is out. The results establish a possibility of spectral gaps and provide new computational tools for studies of 3D photonic crystals. A. Figotin and Yu. Godin, "Spectral Properties of Thin-film Photonic Crystals", SIAM J. Appl. Math., 61, No. 6, pp. 2008-2035 (2001). We finished our work on nonlinear photonic crystals with quadratic nonlinearity including the role of the group velocity matching for nonlinear interactions in periodic media. We can see looking at publications a growing interest to nonlinear periodic dielectric structures, especially with quadratic nonlinearity. We believe that the work we have conducted is an achievement in that area. We learned from the editor that our paper was "one of the most accessed articles for the Journal last year". A. Figotin and A. Figotin "Nonlinear Photonic Crystals. I. Quadratic Nonlinearity", Waves in Random Media, II, pp. R31-R102 (2001). The work on the development of computationally efficient "Resolvent method" for localized states in 2D photonic crystals of the square geometry is completed. We believe that the proposed method is superior in both the speed and the accuracy of computation. A. Figotin and V. Curen, "Resolvent Method for Computation of Localized Defect, Modes of H-polarization in 2D Photonic crystals, Phys. Rev. E, 64, 056623, 2001. Rev. E, Vol. 63, pp. 066609-1-066609-17, 2001. All the computational work was carried out on our 581 "Octane" computers as well as 32 CPU parallel 581 "Origin 2000" computer.			
14. SUBJECT TERMS			15. NUMBER OF PAGES 19
			16. PRICE CODE
17. SECURITY CLASSIFICATION OF REPORT	18. SECURITY CLASSIFICATION OF THIS PAGE	19. SECURITY CLASSIFICATION OF ABSTRACT	20. LIMITATION OF ABSTRACT

20020816 043

## Nachman Arje Civ AFRL/AFOSR

---

**From:** Alexander Figotin [afigotin@uci.edu]  
**Sent:** Monday, July 22, 2002 6:12 PM  
**To:** Nachman, Arje  
**Cc:** Nancy Kelly; Soo Lee; jbermude@uci.edu  
**Subject:** Final Report, 2002, for Contract No. F49620-99-1-0203.

Dear Arje,

Please find below my Final report for Contract No. F49620-99-1-0203.

Please confirm the receipt of the message.

Thank you, Alex Figotin.

-----  
Final Report, 2002, for Contract No. F49620-99-1-0203.

1. Title: ''Tunable Photonic Crystals''.
2. AFOSR Contract No. F49620-99-1-0203.
3. Final Report for the period October 1, 1999 - May 31, 2002.
4. PI Name: Alexander Figotin, Department of Mathematics, University of California at Irvine

Irvine, CA 92697-3875. Phone: 949-824-5506. Fax: 949-824-7993.

E-mail address: afigotin@uci.edu  
-----

### I. OBJECTIVES.

1. Develop time efficient and reliable methods for the computation of the band gap structures for 2D photonic crystals of the general geometry and 3D photonic crystals with cubic geometry. Develop asymptotic theory of 3D thin-film photonic crystals.
  2. Develop the theory of nonlinear interactions in 1D, 2D and 3D photonic crystals.
  3. Develop the methods for the computations of the localized eigenmodes and their frequencies generated by the defects in photonic crystals.
  4. Develop the theory on magnetic photonic crystals. Applications of magnetic photonic crystals.
  5. Explore the applications of magnetic photonic crystals in submillimeter range of frequencies.
- 

### II. STATUS OF EFFORT

1. Our initial theoretical work with Dr. Yu. Godin on asymptotic models for 3D thin-film photonic crystals is out. The results establish a possibility of spectral gaps and provide new computational tools for studies of 3D photonic crystals.

A. Figotin and Yu. Godin, "Spectral Properties of Thin-film Photonic

Crystals", SIAM J. Appl. Math., 61, No. 6, pp. 2008-2035 (2001).

2. We finished our work on nonlinear photonic crystals with quadratic nonlinearity including the role the group velocity matching for nonlinear interactions in periodic media. We can see looking at publications a growing interest to nonlinear periodic dielectric structures, especially with quadratic nonlinearity. We believe that the work we have conducted is an achievement in that area. We learned from the editor that our paper was "one of the most accessed articles for the Journal last year".

A. Babine and A. Figotin "Nonlinear Photonic Crystals. I. Quadratic Nonlinearity", Waves in Random Media, 11, pp. R31-R102 (2001).

3. The work on the development of computationally efficient "Resolvent method" for localized states in 2D photonic crystals of the square geometry is completed. We believe that the proposed method is superior in both the speed and the accuracy of computation.

A. Figotin and V. Goren, "Resolvent Method for Computation of Localized Defect, Modes of H-polarization in 2D Photonic crystals, Phys. Rev. E, 64, 056623, 2001.

4. Our theoretical results on magnetic photonic crystals have been completed and published. The results can have important applications for more efficient and of smaller dimensions antennas.

A. Figotin and I. Vitebskiy, "Spectra of Periodic Nonreciprocal Electric Circuits", SIAM J. Appl. Math., 61, No. 6, pp. 1959-1979 (2001).

A. Figotin and I. Vitebskiy, "Nonreciprocal Photonic Magnetic Crystals", Phys. Rev. E, Vol. 63, pp. 066609-1 -066609-17, 2001

6. All the computational work was carried out on our SGI "Octane" computers as well as 32 CPU parallel SGI "Origin 2000" computer.

Dr. Godin and Dr. Goren have written the codes for the parallel computer and use of the parallel computer became routine.

-----

### III. ACCOMPLISHMENTS/NEW FINDINGS.

1. Our work with Dr. Vitebskiy on nonreciprocal (gyrotropic) photonic crystals has shown that one can achieve strong nonreciprocity just by proper arrangements of common and widely available dielectric materials.

Here are the main attractive features of microwave, millimeter, and submillimeter devices utilizing our invention:

- substantially smaller weight and dimensions
- multifold enhancement in power capabilities
- tunability
- excellent survivability
- functionality under harsh external conditions including: temperature, impacts and blows, vibrations, any radiation
- versatility

The theory of those structures are described in our Phys. Rev. E paper with Dr. Vitebskiy.

2. Our work with Dr. Babine on the nonlinear photonic crystals provides solid theoretical base for the studies of a number on nonlinear regimes in periodic dielectric structures. Based on the Stationary Phase Method applied to oscillatory interaction integrals arising in nonlinear Maxwell equations, we described all important selection rules of stronger nonlinear interactions, and developed a quantitative classification of nonlinear interactions.

In particular, we have shown the for regimes under study the group velocity matching, not the frequency matching (as commonly believed), is the most important selection rule.

-----

#### IV. FACULTY SUPPORTED:

Dr. A. Babine, Dr. Yu. Godin, Dr. V. Goren and Dr. I. Vitebskiy.

-----

#### V. PUBLICATIONS and SUBMITTED PAPERS for the reported period:

(1) A. Figotin and Yu. Godin, "Spectral Properties of Thin-film Photonic Crystals", SIAM J. Appl. Math., 61, No. 6, pp. 2008-2035 (2001).

(2) A. Figotin, Yu. Godin, I. Vitebskiy, "Tunable Photonic Crystals" in "Material Research Society Symposium Proceedings", Vol. 603, 1999 Material Research Society, KK6.1.1-KK6.1.6. (We learned that the paper is out in the reported period).

(3) A. Babine and A. Figotin "Nonlinear Photonic Crystals. I. Quadratic Nonlinearity", Waves in Random Media, 11, pp. R31-R102 (2001).

(4) A. Figotin and V. Goren, "Resolvent Method for Computation of Localized Defect, Modes of H-polarization in 2D Photonic crystals, Phys. Rev. E, 64, 056623, 2001.

(6) A. Figotin and I. Vitebskiy, "Spectra of Periodic Nonreciprocal Electric Circuits", SIAM J. Appl. Math., 61, No. 6, pp. 1959-1979 (2001).

(7) A. Figotin and I. Vitebskiy, "Nonreciprocal Photonic Magnetic Crystals", Phys. Rev. E, Vol. 63, pp. 066609-1 -066609-17, 2001.

-----

#### VI. CONFERENCES and INVITED TALKS:

A. Figotin, "Spectral Theory and Oscillatory Integrals in Nonlinear Interactions", International Workshop on Mathematical Physics, Brazil, Mambucaba, August 19 - 25, 2001

I. Vitebskiy, "Gyrotropic Photonic Crystals", Condensed Matter Theory Seminar, UCI, May 2001.

A. Figotin, "Nonlinear Wave Interactions in Periodic Media", AMS conference, Los Vegas, April 21-22, 2001

A. Figotin, "Three-dimensional Thin-Film Photonic Crystals", Electromagnetics Workshop, Brooks Air Force Base, San Antonio, January 2000

A. Figotin, "Spectral Theory in Nonlinear Wave Interactions",  
AMS conference, Birmingham, Alabama; November 10-12, 2000

A. Babine, "Nonlinear Phenomena in Periodic Dielectric Media",  
2000 AFOSR Workshop on Nonlinear Optics, Tucson, September 2000.

International Workshop "Quantum Spectra and Dynamics", Israel,  
"Nonlinear phenomena in periodic dielectric media", July 2000,  
A. Figotin.

Weizmann Institute, Rehovot, Israel,  
"Nonlinear phenomena in periodic dielectric media", July 2000,  
A. Figotin.

Electromagnetics Workshop, Brooks Air Force Base, San Antonio,  
"Wave Propagation in Weakly Nonlinear Periodic Media", January 2000,  
A. Figotin

"Material Research Society Symposium, "Photonic Crystals", November,  
1999,  
A. Figotin & I. Vitebskiy

The Second International ISAAK 99 Congress, Japan ,  
"Spectral Theory in Weakly Nonlinear Periodic Media", August, 1999,  
A. Figotin

Air Force Institute of Technology, Wright-Peterson Air Force Base,  
Dayton, Ohio, "Wave Propagation in Weakly Nonlinear Periodic Media",  
July, 1999, A. Figotin

International AMS Summer Research Conference  
"Wave Phenomena in Complex Media",  
"Spectral Theory in Weakly Nonlinear Periodic Media", June, 1999, A.  
Figotin.

Department of Mathematics, Southern Methodist University, Dallas, TX.  
Mathematical modeling of photonic crystals.  
September 20, 2000, Yu. Godin.

Steklov Institute of Mathematics at St.Petersburg, Russia.  
Spectral properties of thin-film photonic crystals.  
July 28, 2000, Yu. Godin.

Corning Scientific Center in St.Petersburg, Russia.  
Tunable photonic crystals.  
July 21, 2000, Yu. Godin.

Physico-Technical Ioffe Institute, St.Petersburg, Russia.  
An asymptotic model of three-dimensional photonic crystal.  
July 20, 2000, Yu. Godin.

WAVES 2000: 5-th International Conference on Mathematical and Numerical  
Aspects of Wave Propagation.Santiago de Compostela, Spain.  
Asymptotic model of Three-Dimensional Photonic Crystal.  
July 10--14, 2000, Yu. Godin.

Facultad de Ciencias, Universidad Autonoma de Madrid, Spain.  
Theory of spectra of thin-film photonic crystals.  
July 6, 2000, Yu. Godin.

Fisica I Enginyeria Nuclear, Universitat Politecnica de Catalunya,  
Spain.  
Theory of spectra of thin-film photonic crystals.  
July 3, 2000, Yu. Godin.

The Second Irvine Days in Applied and Computational Mathematics,

Calculation of the spectrum of some two- and three-dimensional photonic crystals.

May 14, 2000, Yu. Godin.

Nuclear Research Center Soreq, Israel.

Calculation of the spectrum of some two-dimensional photonic crystals.

July 14, 1999, Yu. Godin.

Physics Department, Van der Waals-Zeeman Institute, University of Amsterdam, Netherlands.

Calculation of the spectrum of some two-dimensional photonic crystals.

July 9, 1999, Yu. Godin.

Seminaire de Physique mathematique et Geometrie, Universite Paris 7, France.

Calculation of the spectrum of some two-dimensional photonic crystals.

July 7, 1999, Yu. Godin.

Department of Physics, University of Bath, United Kingdom.

Calculation of the bandgap structure of some two-dimensional photonic crystals.

July 1, 1999, Yu. Godin.

Department of Mathematics, University of Liverpool, United Kingdom.

Calculation of the spectrum of some two-dimensional photonic crystals.

June 29, 1999, Yu. Godin.

-----

## VII. Patents.

We filed the provisional patent application

UC Case No. 2001-350-1

"Gyrotropic Photonic Crystal and Applications for the Same"  
acknowledging the support of AFOSR.

The patent is related to our recent results on magnetic photonic crystals.

-----

## VII. INTERACTIONS/TRANSITIONS.

Our work on nonreciprocal and magnetic photonic crystals received an attention from the industry.

We established working relations with Dr. D. Barker from Raytheon, and arranged a meeting with a group of Dr. G. Schultz from Boeing.

We had a meeting with a group of representatives from Raytheon in January 2001 in UCI, Office of Technology Alliances. The subject of the meeting was potential applications of nonreciprocal (gyrotropic) photonic crystals to microwave devices with enhanced performance and of smaller dimensions. It is my impression that Dr. Barker and Raytheon's attorney recognized a significant potential of proposed by us new dielectric structures. UCI provided all necessary documents to establish research partnership with Raytheon.

A similar meeting took place with representatives of Boeing, including Dr. G. Schultz, in Boeing West Hills Laser & Electro Optical Systems.

Dr. Schultz indicated an interest not only to applications of our work to devices of traditional frequencies but also to optical frequency range. This indicates that what used to be just a theoretical possibility

may be today practical enough for utilization in useful devices.